
Automata and Formal Languages

Due December 16, 2014 before class!

Exercise 1 (FO - 10 points)

Give first-order sentences describing the languages induced by the following regular expressions:

- (a) $r_1 = a^*$
- (b) $r_2 = \Sigma^* a \Sigma$
- (c) $r_3 = \Sigma^* b a^* b \Sigma^*$
- (d) $r_4 = a(ba)^*$

Exercise 2 (MSO I - 10 points)

Come up with MSO sentences describing the following languages:

- (a) L_1 : The language of word where 'a's only occur in even positions.
- (b) L_2 : The language of words that have even length and consist of 'a's only.
- (c) L_3 : The language containing an even number of 'a' between two occurrences of 'b's.

Exercise 3 (MSO II - 10 points)

Describe the languages given by the following formulae verbally and construct an automaton recognizing them.

- (a) $\exists x : first(x)$
- (b) $\neg \exists x : \exists y : x < y \wedge Q_a(x) \wedge Q_b(y)$
- (c) $\forall x : (Q_b(x) \Rightarrow \exists y : (x < y \wedge Q_a(y)))$

Exercise 4 (MSO III - 10 points)

Prove: In MSO-formulae we can eliminate $<$.